

# Solving Polynomial Equations (Finding Zeros)

## 1. Try Factoring

- a. Greatest Common Factor
- b. Count Terms
  - i. 2 Terms – Special Patterns
    1. Difference of Squares:  $a^2 - b^2 = (a - b)(a + b)$
    2. Sum of Cubes:  $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
    3. Difference of Cubes:  $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$
  - ii. 3 Terms – ( ) ( )
  - iii. 4 Terms – Grouping
- c. Try to factor more
- d. To find zeros, set each factor = 0 and solve (end of problem)

## 2. $p$ 's and $q$ 's

- a. List  $p$  (factors of constant term) and  $q$  (factors of leading coefficient) and all possible  $\frac{p}{q}$
- b. Use a graph to find an  $x$ -intercept
- c. Use synthetic division with the  $x$ -intercept to verify that it is a zero
- d. If the depressed polynomial is a quadratic, solve it (end of problem)
  - i. Otherwise, repeat step 2b - 2d with the depressed polynomial
- e. Factors are in form  $(x - k)$  where  $k$  is a zero

**Factor the Greatest Common Factor, then find the zeros.**

1.  $3x^2 + 5x$
2.  $4x^3 + 16x$

**Try to factor the Greatest Common Factor, then factor the binomial, then find the zeros.**

3.  $4x^2 - 9$
4.  $2x^3 + 16$
5.  $125x^3 - 1$

**Try to factor the Greatest Common Factor, then factor the trinomial, then find the zeros.**

6.  $x^2 + 5x + 6$
7.  $2x^2 - 6x - 8$

**Try to factor by grouping, then find the zeros.**

8.  $x^3 + 5x^2 - 2x - 10$

**Try to factor, if you cannot, use  $p$ 's and  $q$ 's to factor, then find the zeros.**

9.  $x^3 - 7x - 6$
10.  $3x^4 + 2x^3 + 2x^2 + 2x - 1$

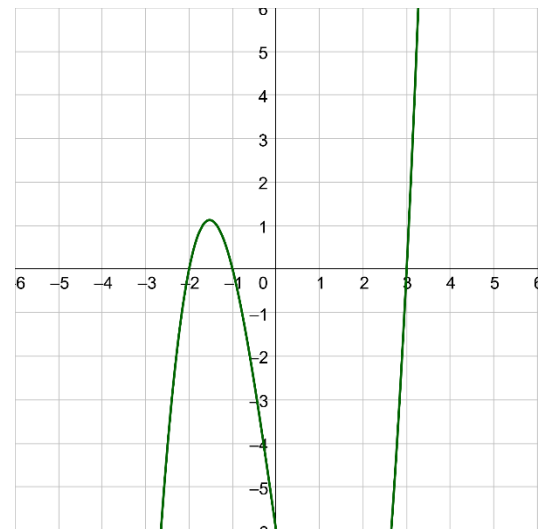


Figure 1: Number 9

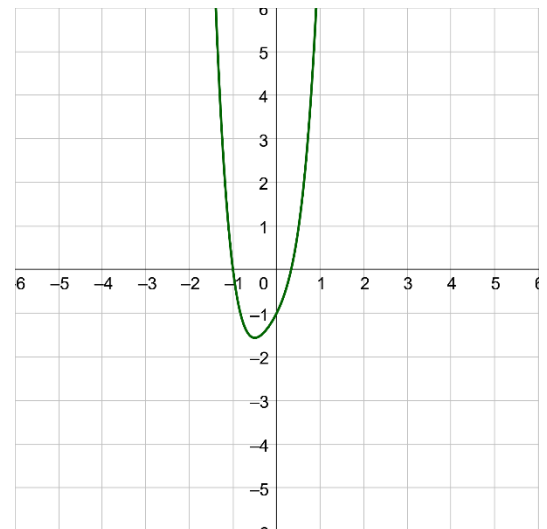


Figure 2: Number 10

Name: \_\_\_\_\_

### Answers

1.  $x(3x + 5); x = 0, -\frac{5}{3}$
2.  $4x(x^2 + 4); x = 0, \pm 2i$
3.  $(2x - 3)(2x + 3); x = \frac{3}{2}, -\frac{3}{2}$
4.  $2(x + 2)(x^2 - 2x + 4); x = -2, 1 \pm \sqrt{3}i$
5.  $(5x - 1)(25x^2 + 5x + 1); x = \frac{1}{5}, \frac{-1 \pm \sqrt{3}i}{10}$
6.  $(x + 2)(x + 3); x = -2, -3$
7.  $2(x - 4)(x + 1); x = 4, -1$
8.  $(x + 5)(x^2 - 2); x = -5, \pm \sqrt{2}$
9.  $(x - 3)(x + 2)(x + 1); x = 3, -2, -1$
10.  $(3x - 1)(x + 1)(x^2 + 1); x = \frac{1}{3}, -1, \pm i$